If we had an index file, we could look it up in the index file under "index file".

— Tegan Jovanka [Janet Fielding], "Castrovalva (Part 1)", Doctor Who, Season 19 (January 4, 1982)

I started with the phone book. Looking up "mensa" was not going to be easy, what with having to follow the strict alphabetizing rules that are so common nowadays. I prefer a softer, more fuzzy alphabetizing scheme, one that allows the mind to float free and "happen" upon the word. There is pride in that. The dictionary is a perfect example of over-alphabetization, with its harsh rules and every little word neatly in place. It almost makes me never want to eat again.


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Dicebat Bernardus Carnotensis nos esse quasi nanos gigantium humeris insidentes, ut possimus plura eis et remotiora videre, non utique proprii visus acumine, aut eminentia corporis, sed quia in altum subvehimur et extollimur magnitudine gigantea.

[Bernard of Chartres used to say that we were like dwarfs seated on the shoulders of giants. He pointed out that we see more and farther than our predecessors, not because we have keener vision or greater height, but because we are lifted up and borne aloft on their gigantic stature.]

— John of Salisbury, Metalogicon (1159), translated by Daniel D. McGarry (1955)

The secret to productivity is getting dead people to do your work for you.

— Robert J. Lang (2009)

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We should explain, before proceeding, that it is not our object to consider this program with reference to the actual arrangement of the data on the Variables of the engine, but simply as an abstract question of the nature and number of the operations required to be performed during its complete solution.

— Ada Augusta Byron King, Countess of Lovelace, translator’s notes for Luigi F. Menabrea, “Sketch of the Analytical Engine invented by Charles Babbage, Esq.” (1843)

How to play the flute. [picks up a flute] Well, here we are. You blow there and you move your fingers up and down here.

— Alan [John Cleese], “How to Do It”, Monty Python’s Flying Circus, episode 28 (aired October 26, 1972)

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This index includes only algorithms with explicit pseudocode; see the main index for other named algorithms.

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A wisely chosen illustration is almost essential to fasten the truth upon the ordinary mind, and no teacher can afford to neglect this part of his preparation.

— Howard Crosby (c.1880)

One showing is worth a hundred sayings.

— Alan Watts (misquoting a Chinese proverb), The Way of Zen (1957)

Please do not think that this is a neutral matter and that the only advantage of doing without pictures is that of saving space. Pictures in textbooks actually interfere with the learning process.

— Neville Martin Gwynne, Gwynne’s Grammar (2013)

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1. Have something to say.
2. Say it.
3. Stop when you have said it.
4. Give the paper a proper title.

— John Shaw Billings, "An Address on Our Medical Literature",
International Medical Congress, London (1881)

You know, I could write a book.
And this book would be thick enough to stun an ox.


Colophon

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