

1. Suppose we are given a set S of n line segments in the plane, each of which is either horizontal or vertical. Each horizontal segment $h \in S$ is specified by its left x -coordinate $h.l$, its right x -coordinate $h.r$, and its y -coordinate $h.y$. Each vertical segment $v \in S$ is specified by its x -coordinate $v.x$, its bottom y -coordinate $v.b$, and its top y -coordinate $v.t$. Assume that all x - and y -coordinates are distinct.

Describe and analyze an algorithm to compute the number of pairs of segments in S that intersect. (Because all coordinates are distinct, if two segments in S intersect, one must be horizontal and the other vertical.)

[Hint: You can do better than blindly applying Homework 9.]

**The remaining problems are for you play with on your own.
Discussion in office hours or on Discord is welcome, but don't submit solutions!**

2. Suppose we are given a set S of n line segments in the plane, each of which is either horizontal or vertical. Each horizontal segment $h \in S$ is specified by its left x -coordinate $h.l$, its right x -coordinate $h.r$, and its y -coordinate $h.y$. Each vertical segment $v \in S$ is specified by its x -coordinate $v.x$, its bottom y -coordinate $v.b$, and its top y -coordinate $v.t$. Suppose we are also given two points s and t in the plane, each specified by their x - and y -coordinates. Assume that all x - and y -coordinates are distinct.
 - (a) Suppose neither s nor t lies on any segment in S . Describe and analyze an algorithm to decide whether there is a path from s to t in the plane that does not intersect any segment in S . (Think of the segments in S as *walls*.)
 - (b) Suppose both s and t lie on (different) segments in S . Describe and analyze an algorithm to decide whether there is a path from s to t in the plane that lies entirely in the union of segments in S . (Think of the segments in S as *roads*.)
 - * (c) Solve both of these problems in $O(n \text{ polylog } n)$ time.
3. Suppose you are given a set R of axis-aligned rectangles in the plane. Each rectangle $r \in R$ is specified by its left x -coordinate $h.x$, its right x -coordinate $h.r$. Assume all coordinates are distinct.
 - (a) Find a point p that lies in the largest number of rectangles in R .
 - (b) Find the largest nested sequence of rectangles in R .